

PAPER

Mapping atomic motions with ultrabright electrons: towards fundamental limits in space-time resolution

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The long held objective of directly observing atomic motions during the defining moments of chemistry has been achieved based on ultrabright electron sources that have given rise to a new field of atomically resolved structural dynamics. This class of experiments requires not only simultaneous sub-atomic spatial resolution with temporal resolution on the 100 femtosecond time scale but also has brightness requirements approaching single shot atomic resolution conditions. The brightness condition is in recognition that chemistry leads generally to irreversible changes in structure during the experimental conditions and that the nanoscale thin samples needed for electron structural probes pose upper limits to the available sample or “film” for atomic movies. Even in the case of reversible systems, the degree of excitation and thermal effects require the brightest sources possible for a given space-time resolution to observe the structural changes above background. Further progress in the field, particularly to the study of biological systems and solution reaction chemistry, requires increased brightness and spatial coherence, as well as an ability to tune the electron scattering cross-section to meet sample constraints. The electron bunch density or intensity depends directly on the magnitude of the extraction field for photoemitted electron sources and electron

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1 energy distribution in the transverse and longitudinal planes of electron propagation. This
work examines the fundamental limits to optimizing these parameters based on relativistic
5 electron sources using re-bunching cavity concepts that are now capable of achieving 10
femtosecond time scale resolution to capture the fastest nuclear motions. This analysis is
given for both diffraction and real space imaging of structural dynamics in which there are
several orders of magnitude higher space-time resolution with diffraction methods. The
10 first experimental results from the Relativistic Electron Gun for Atomic Exploration
(REGAE) are given that show the significantly reduced multiple electron scattering
problem in this regime, which opens up micron scale systems, notably solution phase
chemistry, to atomically resolved structural dynamics.

1 Introduction

15 One of the long standing objectives in science has been to have sufficient spatial
and temporal resolution to directly watch atomic motions during the primary
motions governing structural transitions.^{1,2} This quest is relevant to helping
understand at the atomic level of detail, effectively, all classes of structural
20 transitions from issues of condensed matter physics of strongly correlated
electron-lattice materials, extreme states of matter, and biological functions. In
chemistry, this objective is central to the discipline. The very notion of a chemical
process involves the passage of a system from one stable structure to another in
which the chemist tries to control conditions to direct the desired process over the
25 myriad of other possible outcomes. The ability to control chemistry largely resides
in arranging conditions to lower the barrier and entropic factors to favour a
particular chemical pathway. The intellectual pursuit of chemistry is to under-
stand the factors that control barrier heights, within the context of a complex
many body potential, and to connect molecular structure to macroscopic prop-
30 erties. This statement is intended to include advances in *ab initio* theory, synthetic
strategies, and experimental methods to probe different aspects of the system and
system-bath interactions driving chemistry. The unifying concept in this pursuit
is to try to identify the key atomic motions that lead the system over the barrier
region, or stated differently to picture the transition state region, the critical
35 “point of no return” that connects the reactant to the product free energy surfaces.
A direct observation of atomic motions during the transition from one structure
to another would provide the most rigorous test possible for various concepts that
have evolved for inferring chemical pathways. We could see this directly. This
objective has now been met.³⁻⁵ The recent development of ultrabright electron
40 and X-ray sources to provide the necessary structural probes have opened up the
femtosecond time domain to atomically resolved dynamics.²⁻⁸ The source tech-
nology is rapidly advancing to enable atomic imaging of structural dynamics of
ever larger and more complex systems. There are, however, fundamental limits to
source brightness and sample issues that need to be overcome to apply this new
45 imaging modality to problems of general interest.

For the purpose of this discussion, we will focus on source requirements with
respect to spatial and temporal resolving power to study molecular systems
undergoing chemical reactions. With respect to time resolution, the relevant time
50 scales to this problem have been well appreciated since the first connection of
microscopic processes to reaction rates in the quest for an absolute rate theory.⁹

1 This work ultimately led to the development of transition state theory. The
defining moment of chemistry is captured in the discussion of barrier crossing
processes. This time scale varies for different systems but is on the order of few 10
5 s of femtoseconds (fs; $1 \text{ fs} = 10^{15} \text{ s}$) to 100 femtosecond time scales. There are
faster motions in nature. For example, the OH stretch of water has a period of 10
fs but the motions involved are less than 0.05 \AA , hardly chemically relevant. The
time scale is defined by the relevant motions over length scales corresponding to
10 0.1 to 1 \AA , leading to distinct changes in structure. More specifically, these
motions must in turn be coupled to the nuclear continuum of states to relax the
system to a displaced minimum in the many body potential corresponding to a
long lived state or stable product state. There must be damping or energy dissipation
15 in the process to relax on the product surface. It is the approximately 100 fs
time scale of relaxation along a reaction coordinate that dictates the required time
resolution. It is important to realize that not all motions are equally coupled to the
reaction coordinate and the degree of coupling rapidly evolves in the barrier
crossing region.⁴ The highly anharmonic nature of the many body interactions at
this far from equilibrium point in nuclear configuration space leads to strong
20 mixing of the otherwise suitable normal mode basis to describe equilibrium
fluctuations. Normal modes are accurate descriptions of atomic motions for
small excursions over which the potential is well approximated to be harmonic,
i.e. the nuclear fluctuations are within linear response limits. The far from
equilibrium fluctuations that sample the barrier crossing region are highly
25 nonlinear and the most anharmonic modes tend to be the low frequency modes
that undergo the largest relative motions. These modes are also the most highly
damped as they occur within the highest spectral density of modes for conserving
energy and momentum in the relaxation process.^{10,11} It is the net excursion along
the modes most strongly coupled to the reaction coordinate that define the
relevant time scales of chemistry. These modes, whether involving intramolecular
30 processes, solvent controlled chemistry, or the chemistry controlled by protein
environmental fluctuations, tend to be in the 100 cm^{-1} frequency range, which
gives rise to the generalized requirement of 100 fs time resolution to capture the
chemistry.⁴

35 The spatial resolution requirements are equally challenging in that one needs
sub- \AA spatial resolution to pull out the important relative motions directing
atomic displacements from one stable structure to another. To a first approxi-
mation, the spatial resolution requirement exceeds that needed for static structure
determination. For example, in the photo-isomerization of retinal, the
40 primary event involved in vision and energy transduction within the rhodopsin
family of proteins, the key motions are on the order of 0.1 \AA for the carbon atoms
at the central bond axis of the isomerization.¹² Save in the act of bond dissociation,
chemically relevant motions are between 0.1 and 1 \AA . To fully resolve the
primary motions requires either hard X-rays or high energy electron probes with
45 sufficiently short carrier wavelengths to resolve these motions. Even so, this level
of spatial resolution would be out of range for most sources, however, time-
resolved measurements involve differential measurements. The initial structure
is known. It is only the relative changes from this known starting point that need
to be resolved, not the entire structure for every atomic position to this level of
50 accuracy. The key to being able to resolve chemically relevant motions is that the
source serving as the structural probe must be sufficiently stable and bright

1 enough to render signal to noise ratios (SNR) sufficient to pull out these small
relative changes in intensity that report the atomic positions. The most sensitive
method for determining atomic structure is the use of diffraction methods or
5 imaging in reciprocal space. This observable takes advantage of the N^2 ampli-
fication of the diffracted signal intensity by scattering off N identically arranged
molecules to amplify the scattered signal. The criteria of high brightness and high
stability for the source reduce to achieving sufficient signal to noise ratios in the
diffracted orders to pull out the structural changes of interest. The quality of
10 sample often plays a deciding factor in the achievable resolution; however, it is
only recently that the sources serving as structural probes have reached the level
of brightness where sample issues are the main bottleneck.

Differential detection of the structural changes is achieved by comparing the
changes in structure following an excitation pulse, which triggers the structural
change of interest. Here, it needs to be fully appreciated that, in the absence of a
15 “trigger”, the act of barrier crossing driven by background thermal noise is a rare
event. For even small barriers (*e.g.* 1 eV), there are less than $1 : 10^8$ molecules
undergoing a barrier crossing event at any instant in time.⁴ In principle, one could
track the motions of an individual molecule undergoing first order reactions, or
molecular collision partners for second order processes, to observe such crossings
20 but the ability to observe such motions and the enormity of collecting sufficient
atomic images at the required framing rate to get above background noise, never
mind increased demands on source brightness, make this prospect intractable.
The processes of interest must be optically triggered to observe the key relative
atomic motions connecting two stable structures within the complex, highly
25 dimensional, potential energy surfaces of interest to chemistry. This simple
realization has a number of important consequences for the conduct of the
experiment. First, the perturbation used to trigger the chemistry must be faster
than the ensuing motions of interest. Only femtosecond laser excitation meets
this requirement. Furthermore the optical excitation must prepare the system on
30 excited state surfaces that intersect reactive crossings under barrierless condi-
tions. If there is a barrier in the excited state, the time scale for the buildup of the
product state is much slower than that of the primary motions involved. In the
presence of a barrier, the system will reach a thermal equilibrium within the
vibrational modes corresponding to the excited state surface. In this event, there
35 are uncorrelated, thermally, sampled crossings and the details of the relevant
motions will not be resolved. The problem reverts to the same statistics as trying
to capture barrier crossing events along the ground state. This requirement for a
barrierless excited state process not only limits the number of potentially trac-
table systems for study but has additional consequences. To observe the relevant
40 motions above the background of unexcited molecules requires that on the order
of 10% of the molecules or lattice sites are undergoing the photo induced
structural change. The quantum yield for the desired photo process must be at
least this large and there is an upper limit to the degree of excitation. The <100
45 femtosecond requirements for the excitation pulse necessarily leads to high peak
powers, however, the peak power must be maintained at excitation levels on the
order of 100 GW cm^{-2} or lower to avoid multi photon ionization artifacts.¹³
Basically, above this peak power multi photon processes begin to dominate and
even the degree of state preparation becomes ill defined as multi photon excita-
50 tion to higher lying excited states begin to also significantly contribute. For typical

1 molecular densities, this latter condition means that samples must be on the
order of a few microns or thinner or else the required excitation levels (>10%
5 photoproduct formation) lead to excessively high incident peak powers. These are
nontrivial sample constraints as one must have sufficient surface area within this
thickness restriction to attain adequate signal to noise to stitch together a movie
of the atomic motions involved in the process of interest.

Of all the above discussed requirements, the most limiting is the requirement
for approximately 10% of the system to be undergoing the phototriggered
10 structural transition. Apart from gas phase systems, which can be rapidly
exchanged between laser shots, this level of excitation leads to sample damage in
a single shot. This statement is especially true for single crystals that give the
highest structural resolution. Normally in diffraction experiments, the upper
15 limit for source brightness is determined by X-ray or electron induced damage. In
this class of experiments, the main limitation with respect to sample damage is
not the structural probe but the excitation process to trigger the chemistry that
damages the sample. It is not enough to have simultaneous atomic resolution
with 100 fs time resolution or less but one must attain this experimental
20 parameter space within single shot conditions. Herein lies the real challenge. The
source brightness for the structural probe must not only be capable of high space-
time resolution but of sufficient intensity to achieve atomic resolution at or
approaching single shot conditions.^{4,14}

Enormous gains in source brightness have been achieved for both electron and
X-ray sources to meet this condition. The major advance in X-ray source bright-
25 ness was achieved through technical advances made in undulator technology that
enabled scaling the free-electron laser concept to the X-ray range. These sources
are referred to as 4th generation light sources or X-Ray Free Electron Lasers
(XFELs). In comparison to 3rd generation synchrotron sources, XFELs represent
an increase in source brightness of over almost ten orders of magnitude.⁷ XFELs
30 are not true laser resonators but are based on self amplification of spontaneous
emission or SASE sources. As with SASE sources in the visible range, there are
huge stochastic fluctuations in intensity and spectrum that make shot to shot
normalizing essential to improve the SNR. In addition, there are time jitter issues,
with respect to synchronizing the laser excitation used to trigger structural
35 changes and the RF phase of the electron acceleration, that gives rise to 200 fs
timing jitter. In principle, XFELs are capable of <50 fs time resolution using time
stamping methods as another normalization step to extract the time dependent
changes in diffraction efficiency.¹⁵ To date, time-resolved structural dynamics on
the prerequisite time scales (100 fs to picosecond) have not been realized with
40 sufficient numbers of diffraction orders to follow structural changes. There has
been a recent report of resolved structural changes, albeit not the actual transient
structures, on the microsecond time scale¹⁶ and studies of a single diffraction
order have been used to infer the role of the lattice in directing material properties
for strongly correlated electron lattice systems.¹⁷ There remain a number of
45 technical challenges in the normalization procedures required to attain sufficient
SNR and also in the large number of crystal projections needed for X-ray structure
determination, prior to the onset of X-ray induced damage, that have hindered
efforts in this direction. Further, these sources are not dedicated facilities to this
50 line of inquiry. The most important application for XFELs appears to be in the use
of the high spatial coherence and brightness to enable nano- to micro-protein

1 crystallography, prior to the onset of X-ray induced damage.⁸ Recent develop-
ments in self-assembly of up to M-pixel crystal arrays or photochips^{18,19} (solid
target solution to sample delivery) and aerosol injectors to give random orienta-
tions²⁰ may solve the last technical obstacle in providing a general solution for
5 collecting sufficient reciprocal space to stitch together atomic movies on the
femtosecond time scale.

With respect to electron sources, there are inherent electron–electron repul-
sion or space charge effects that limit source brightness. This problem was readily
10 appreciated and it was felt that it would not be possible to achieve the needed
brightness with electron sources. In this regard, there have been proposals to
achieve the necessary space-time resolution with low intensity sources, with
single electron pulses being the ultimate limit to completely avoid space charge
limits in time resolution.^{21,22} The basic problem is that one needs approximately
15 10^5 to 10^6 electrons to have sufficient SNR to invert diffraction patterns to
structures and approximately 2–3 orders of magnitude more for real space
imaging. In the single electron limit, this requirement translates to over 10^8
photoexcitation events in the data collection process. It is not possible to have
sufficient sample area for such a large number of excitation events, save for gas
20 phase samples where other issues have limited the time resolution. One needs
fully reversible systems that can withstand over 10^6 photocycles between reactive
excited and ground electronic states. The prospect of using single electrons
remains an elusive prospect with respect to achieving simultaneous femtosecond
time resolution and sub-Å spatial resolution to structural transitions. To date,
25 there has only been one report on time resolved dynamics in the single electron
limit in which simple thermally excited acoustic phonons were followed on the
100 ps timescale. This process is fully reversible by its very nature as it does not
involve a structural change. This work rather reinforces the importance of
brightness. In all cases, the brighter the source the better the space-time reso-
30 lution is, as long as the time resolution is sufficient to follow the dynamics of
interest. As will be seen below, ultrabright electron pulses on the order of 10 fs are
now possible, which provides sufficient time resolution to follow even the fastest
nuclear motions. The first atomic movie with sufficient space-time resolution, *i.e.*,
sufficient number of diffraction orders, to resolve the relative atomic motions
35 involved in a structural change was in fact captured with a high brightness
electron source.³ The major advance that made this possible was the realization
that high bunch charge electron pulses do not lose space-time correlation at
sufficient intensities to achieve single shot structure determination. This reali-
zation was made possible through an effectively exact solution to the electron
40 propagation dynamics by solving the coupled equations of motions of some 10^4
electrons,²³ sufficient for the structure determination of systems with simple unit
cells (<3 nm). It was discovered that the transverse velocity spread, related to the
transverse spatial coherence, was not significantly affected. The main issue was
the longitudinal space charge effect. Two solutions were apparent from these
45 calculations. One solution involved the use of extremely short propagation paths
to the sample target to limit pulse broadening to retain 100 fs time resolution.
Here, the key realization was that the transverse coherence, even at short prop-
agation distances with typical transverse velocity spreads, was sufficient for
atomic resolution for systems with unit cells of a few nm. The other solution to
50 emerge from this work was to explicitly exploit the conserved space-time

1 correlation and development of an extremely linear chirp that naturally develops
for nonrelativistic electrons to compress the pulse at the sample position. In this
respect, the electrons at the front of the electron pulse experience electron–electron
5 repulsion effects that lead to acceleration or energy exchange between the
electrons at the back of the pulse that experience deceleration. For nonrelativistic
electrons, the higher energy electrons travel faster than the slow energy electrons.
The electrons at the front stay at the front and the electrons at the back stay at the
back to conserve the original space-time relationship and develop an extremely
10 linear chirp with propagation. This observation led to the proposal for the use of
electric field compression methods or other dispersive elements to compress the
electron pulse.²³ The use of a longitudinal half cycle RF cavity to recompress the
pulse conserves the transverse coherence and appears to be the best solution to
pulse compression for high brightness applications,²⁴ although there are other
15 applications for improved time resolution.²⁵ The overall gains in electron source
brightness over previous low electron density pulsed sources approaches similar
gains as XFELs over prior technology. The compact electron gun design is now
capable of 10^5 to 10^6 electrons per pulse in a 200 fs pulse that is focusable down to
100 micron radius spot sizes typically used in femtosecond laser experiments.²
20 New designs at higher energies will enable <100 fs pulses. The DC-RF pulse
compression concept has achieved approximately a factor of 10 increase in
brightness with attendant technical issues in RF timing jitter that currently limit
the achieved time resolution to approximately 200 fs.^{2,26–28} The time resolution can
be improved to 30 fs with the use of time stamping methods.²⁹ In comparison, the
25 compact electron gun is jitter free. These table top electron sources are excep-
tionally bright. For calibration, taking into account the factor of 10^5 to 10^6 higher
scattering cross-section for electrons over X-rays for the same energy, this source
technology is comparable to 10^{12} X-ray photons per pulse for practical laser
excitation parameters, *i.e.* these electron sources are on par with XFELs in terms
30 of observed signal levels. Here it is important to keep in mind that peak power
limitations require the use of samples on the micron scale or smaller such that
there is little distinguishing differences in sample requirements. The diffraction
efficiency for X-rays is very small for sample thicknesses on the micron scale such
that the observed signal levels are expected to be similar for these two different
35 source technologies. The big differences are that the electron sources are dedi-
cated table top facilities for this class of experiment and are orders of magnitude
more stable than the X-ray counterpart. It is these decided advantages that has
enabled atomic movies of the primary motions involved in structural transitions
to be first captured using electron sources. Advances in laser generated X-ray
40 plasma sources have likewise opened up atomically resolved structural
dynamics on the prerequisite sub-ps timescale.^{30–32} The most important differ-
ence in brightness levels of XFELs sources in relation to all other sources is the
near perfect transverse coherence. This difference makes XFELs the ideal source
for the study of complex large unit cell systems such as proteins; whereas electron
45 sources are currently limited to transverse coherences suitable for the study of
relatively small proteins (<10 nm unit cells). This difference may not hold for long,
as will be discussed in this report. Electron sources have at least 2 orders of
magnitude possible increase in brightness that may even close this gap in
imaging resolution. In this respect, the recent introduction of relativistic electron
50 sources for this application^{33–38} promises to provide the highest spatial-temporal

1 resolution due to the reduction of pulse broadening effects in the relativistic
regime. The full potential of relativistic electron sources to achieve the highest
possible time resolution relies on removing the initial velocity and temporal
5 spread in the RF acceleration phase. This discussion paper focuses on the first
results from the Relativistic Electron Gun for Atomic Exploration (REGAE) that
introduces the use of a rebuncher cavity to achieve the ultimate limit in high
brightness for relativistic electron sources.

10 2 Ultrafast diffraction and real space imaging with relativistic electrons

2.1 Coherence issues: diffraction

15 The focus of this discussion paper is on electron source technology for atomic
imaging dynamics on the primary time scales of chemistry. The image resolution
as with any source is related to both the transverse and spatial coherence of the
source for diffractive imaging or aberrations in the lens system for real space
reconstruction. For X-rays or other light sources, the degree of coherence is
20 defined by the beam divergence, which is a constant after the modality of light
generation is fixed. For electrons, the degrees of transverse and longitudinal
coherence are coupled parameters that depend on the specific space-time
focusing. As an electron pulse is made shorter in duration for a given bunch
charge at some point the space charge effects and spatial inhomogeneity will lead
25 to increased beam divergence or transverse velocity spread and corresponding
loss of in-plane resolution. The transverse spatial coherence is defined by:³⁹⁻⁴¹

$$L_x \approx \lambda/2\pi\sigma_\theta \approx \hbar/\sigma_{p_x}, \quad (1)$$

30 where σ_{p_z} is the angular spread, and σ_{p_x} is given by the transverse momentum
spread. There is a similar relation for the longitudinal coherence, which is
defined as:

$$L_z \approx \hbar/\sigma_{p_z}. \quad (2)$$

35 The longitudinal coherence is only an issue if one wants to coherently
reconstruct an image as in holography. For diffractive imaging, the longitudinal
coherence is not the limiting factor. The coherence length, even for strongly space
charge broadened pulses, is generally much larger than the unit cells of even large
unit cell crystals (>10 nm). Thus, the two most important, coupled, parameters to
40 consider in attaining the required space-time resolution for a particular problem
of interest is to match the transverse coherence to the unit cell of interest for the
spatial resolution and to adjust the electron bunch density accordingly to give the
required electron pulse duration for the time resolution. In the former case, the
required spatial resolution was achieved by adjusting the source size at the
45 photocathode or introducing an aperture to produce an effective source size that
gives a transverse coherence length at the sample position that is a few times the
lateral dimension of the unit cell.⁴¹ In terms of time resolution, the required
spatial resolution limits the bunch density for a given transverse energy spread
50 and the minimum pulse duration on target is achieved by reducing the number of
electrons for a given probe beam size at the sample position, until the

1 longitudinal space charge effects are negligible relative to the time resolution
needed. Again, these parameters are coupled.

5 For most problems of chemical interest, the pulse duration with sufficient
electrons for single shot structure determination is the primary concern. The
shortest electron pulses are achieved with the highest extraction fields as this
minimizes the pulse propagation time to the sample position and thereby
minimizes space charge broadening of the time resolution. The highest extraction
10 fields are achieved with RF acceleration methods that avoid charge accumulation
and breakdown. Extraction fields an order of magnitude larger than DC electron
guns are possible. In addition, as one goes to higher electron energies, there is a
reduction in space charge broadening due to the relativistic correction to the
electron velocities. For first order, in the fully relativistic regime, all the electrons
15 would travel at essentially the same velocity, near the speed of light. In this limit,
the time broadening problem would reduce solely to issues related to the transverse
coherence or transverse velocity spread that would increase with temporal
compression in the longitudinal direction. What are the fundamental limits to
space-time resolution with electrons? There are new developments both in the
20 generation of ultrabright electrons sources for the shortest possible electron pulse
durations/temporal resolution and photocathode concepts that promise to offer
orders of magnitude increases in transverse coherence. These higher energy
electron sources also have greater penetration depths to put sample constraints
completely on par with X-ray sources. We are entering into a new regime for
25 electron sources. The order of magnitude higher field gradients possible with
relativistic electron guns and enormous reduction of longitudinal space charge
broadening in the relativistic regime hold promise to provide the brightest
sources possible for the highest possible spatial-temporal resolution. We high-
light the promise to go beyond present limits in diffraction or reciprocal space
imaging of chemical and biological problems – for which the dynamics are
30 essential to understanding mechanism and functionality.

2.2 Coherence issues: real space imaging – dynamic high energy electron microscopy

35 The incoherent nature of the spatial phase of the electron pulses across the beam
profile presents more difficulties for real space imaging than for diffraction, that
are hard to compensate. To acquire an image with reasonable signal to noise ratio
at the detector position, one aims for 10^6 to 10^7 electrons per acquisition, which
needs to be matched to a typical sample area of a few μm^2 . The electron beam
40 needs to be tightly focused to achieve this density. A tight focus on the other hand
means a reduction of the local coherence length, which calls for an improved total
coherence of the electron pulse from its source on. The photoemitted electron
image at the cathode has to be as close to point-like as possible. Laser spot sizes
below $10\ \mu\text{m}$ are difficult to achieve at the cathode position inside a RF cavity.
45 Typically, the laser is coupled into the cavity from a window several tens of cm
away from the cathode surface, which is insufficient working distance to focus
tighter than 10 microns. It is possible to use structured cathodes to give the
desired source size. However, for current designs, single shot imaging will only be
50 possible with a partially coherent mode and thus relies on Z -contrast (Z = atomic
number) rather than phase contrast. By spatial filtering with an aperture, the

scattered electrons lead to an intensity drop in the imaged electron beam relative to the position of the scattered object for bright-field imaging. In dark field imaging, the unscattered electron beam is stopped by a negative aperture (beam stop) and the scattered electrons are imaged. In both cases, the favorable situation is for each electron to scatter less than once on average. Too little scattering gives low imaging contrast and calls for high electron doses, whereas multiple scattering broadens the minimal spot size of point scatterers in the sample. The number of scattering events depends on the elastic cross-section σ_{el} , which depends on the electrons' energy and the atomic number Z of the scattering material. An approximate expression for σ_{el} is given by:⁴³

$$\sigma_{\text{el}} = \frac{c^2 h^2 Z^{4/3}}{\pi E_0 \beta}, \quad (3)$$

where E_0 is the electron rest energy, and $\beta = v/c$ with the electron's velocity v . The mean free path λ_{el} of an electron in a material with density ρ is related to the cross-section by $\lambda_{\text{el}} = A/N_A \sigma_{\text{el}} \rho$. While the expression for σ_{el} gives a helpful approximation, it can differ from the actual cross-section by a factor of 2. We use the approach presented in ref. 42 to include relativistic corrections in the calculation. In Fig. 1, we compare calculations for the elastic cross-section using the Schrödinger equation, the relativistically corrected Schrödinger equation, as well as the Dirac equation. Solvers for both the relativistic Schrödinger equation and Dirac equation have been implemented into the EDICo-code.⁴⁴ The calculations were performed for unpolarized electrons. We find no significant difference between the relativistic Schrödinger and Dirac result and conclude that effects of spin can be neglected, as also stated in ref. 42. In terms of beam propagation

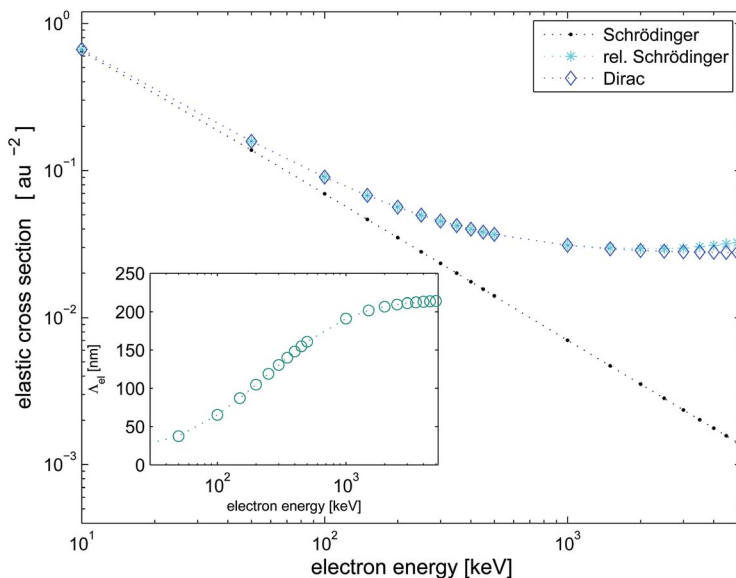


Fig. 1 Comparison of different methods to calculate electron cross-sections in aluminum using the relations given in ref. 42. The inset shows the according mean free path in aluminum for the cross-sections derived from the Dirac equation.

1 through the sample and effect on imaging, the electron beam broadens its energy
distribution in the sample by inelastic collisions. Typically, the total cross-
sections for elastic and inelastic scattering show a qualitatively similar behavior
5 with energy. The ratio $\eta = \sigma_{\text{inel}}/\sigma_{\text{el}}$ was experimentally found to be $\eta = 20/Z^{45}$ and
theoretically $\eta = 26/Z$.⁴³ Since the cross-section for elastic and inelastic scattering
follow similar behavior with energy, η is almost constant in the keV to MeV range.
One can assume that multiple scattering will be reduced by the same factor for
both elastic and inelastic scattering. Damage due to ionization will also be
10 reduced by the same argument, but knock-on damage will be more severe than for
lower energy devices.

When the sample thickness exceeds the mean free path in the material, one
faces two problems in transmission electron microscopy that stem from multiple
scattering: multiple elastic scattering increases the minimal spot size of a point
15 like object; and inelastic scattering similarly leads to aberrations in the recon-
structed real space image. Thus, the resolution will be reduced and distorted.
Such effects are reduced in electron microscopy with relativistic electrons, and
allow in the case of light, low Z , organic materials, the study of micron thick
samples with nanometer resolution. High resolution microscopy with thin
20 samples in which atomic resolution is desired may better be performed in
conventional electron microscopes employing aberration correctors⁴⁶ that are not
currently available for relativistic electron imaging systems.

We studied the feasibility of dynamic real space imaging with pulse propa-
gation simulations in ASTRA. The simulation is launched from the sample
25 position on. A pulse of 10^4 particles with a Gaussian density profile and an energy
of 3 MeV is tracked through the magnetic field of a realistic electromagnetic
solenoid, which is a likely implementation for the objective lens. The solenoid
field was calculated using the CST software suite.⁴⁷ A schematic of the imaging
system implemented in the existing REGAE setup is shown in Fig. 2(a). With the
30 pulse, 500 test particles were used to probe the mean field space charge that travel
along the propagation direction. For a chosen spot size of 10 μm at the sample,
the test particles travel off-center at a distance of 1 μm . The energy spread for the
pulse is chosen to be 2×10^{-4} . The transverse momentum spread of the test
particles was chosen to match scattered electrons up to typical angles of 5 mrad.
35 We performed the simulation for three different focal lengths of 1.1 cm, 5 cm, and
10 cm. The results depending on the bunch charge are presented in Fig. 2(b). We
tracked the test particles until they reached the image plane, and then computed
the RMS width to obtain a point spread function. We find higher resolution for
lower focal lengths, which is to be expected from the respective spherical aber-
40 ration coefficients. Furthermore, we observe a decrease in resolution depending
on charge, which we interpret as the result of the inhomogeneous space charge
field in the bunch, an effect resembling spherical aberrations.⁴⁸ The simulation
has been repeated for different pulse lengths and spot sizes. We find a similar
scaling for all pulse shapes, as visible in Fig. 2(b). In order to reach 1 nm reso-
45 lution the charge must be kept in the fC range. Longer pulses would certainly
relax the issue of space charge induced aberration, as proposed in,^{49,50} but then
additional, higher harmonic cavities need to be employed to decrease the energy
spread that comes with the generation of a long pulse in an RF cavity, which has
50 not been treated in these works.

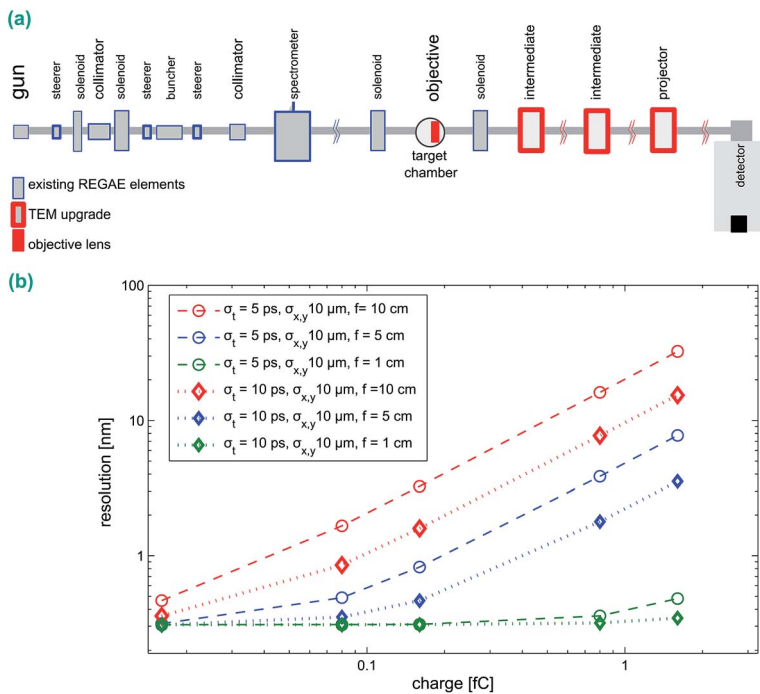


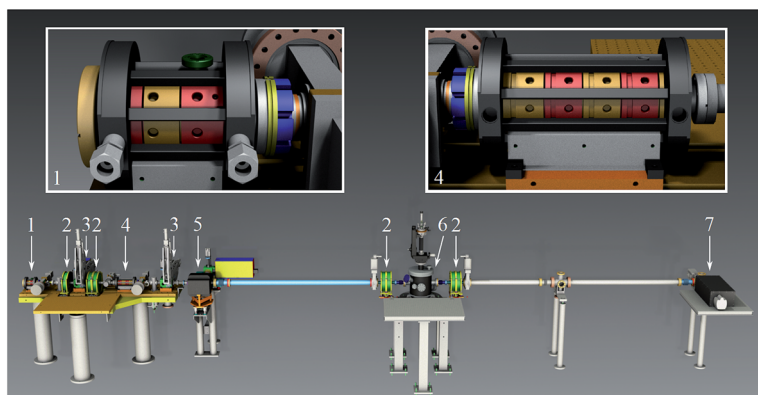
Fig. 2 (a) Schematic of the implementation of a TEM mode within the existing REGAE setup. (b) Effect of charge and objective focal length on resolution for a pulse length of 5 and 10 ps. The beam shape is Gaussian for all cases.

2.3 Electron diffraction with REGAE

2.3.1 The REGAE apparatus. The relativistic electron gun for atomic exploration, REGAE, is a radio frequency (RF) accelerator based gun design operating in a pulsed mode with 50 bursts per second. It is mainly dedicated to the study of structural dynamics in solid, liquid and gas phase of organic and inorganic samples. As elucidated in the introduction, such a device has to fulfill the requirements of short pulses, high brightness, and high coherence at the same time. Electron pulses are created *via* photo-emission by 266 nm, 500 fs pulses of a frequency-tripled Ti:Sa laser impinging the cathode within a 1.5 cell S-band cavity. For the studies presented here, we use either molybdenum, gold, or CsTe as the cathode material. By means of a coaxial on-axis coupler, a travelling 3 GHz S-band wave of some micro-second length launched by a klystron is fed in resonance into the gun cavity, where field gradients of up to 100 MV m^{-1} can be obtained leading to electron energies up to 5 MeV. Running the cavity at high fields has, apart from the beam energy itself, the major advantage that high bunch charge densities can be extracted from the cathode overcoming conventional space charge limitations. Depending on the cathode material and its quantum efficiency, bunch charges in the range from pC for gold and other metal cathodes and 10 pC for CsTe can be extracted. For typical diffraction experiments, we aim for a bunch charges of 100–200 fC (about 1 million electrons) at the target position, as a compromise between beam quality and signal strength. The elements of the beamline are depicted in

1 Fig. 3. The gun section is followed by electro-magnetic solenoids and collimators
5 to shape the beam. The collimators are a critical feature and require a high degree
of engineering to ensure proper alignment under the ultrahigh vacuum
conditions needed to run the RF cavity. These elements are used for collimation and
10 beam clean up as well as to reduce dark current travelling in the beam direction.
One of the most important distinctions of this relativistic electron gun is the low
dark current⁵¹ that is primarily due to the very low base pressure of 10^{-10} mbar
employed in this design concept. Additional beam diagnostic stations allow for
15 determination of transverse electron bunch parameters, *e.g.* beam width, energy,
and energy spread. The beam charge can be detected without disturbing the beam
by means of a resonator, where the electron pulse induces a TM01 mode at 1.3
GHz. The bunch charge can be measured with fC resolution.⁵² The other key
20 feature to this design is the introduction of a rebunching cavity to obtain the
shortest possible pulses at the sample position. The design employs the same
klystron amplifier with an RF splitter to drive both cavities, which requires finding
unique phase solutions for which the pulse is optimally compressed for a given
amplification. The rebunching cavity is designed to temporally refocus the elec-
25 tron pulse at a distance of 5.5 m from the photocathode position. For detection, a
scintillator on a fiber optics plate in the beam line converts the electrons' density
distribution to photons, which are coupled to an EMCCD chip outside of vacuum.
The high dynamic range of the EMCCD combined with its high sensitivity down to
single electron detection allows for simultaneous detection of the undiffracted
beam and diffraction patterns without the necessity for a beam block (Fig. 4).

25 **2.3.2 Beam dynamics and time resolution at REGAE.** The beam dynamics
after the gun are controlled by solenoid magnets, indicated by arrows in Fig. 3.
Depending on the demands on beam size at the sample position and extent of the
diffraction pattern on the detector screen, we either focus the beam through the
30 target on the screen with solenoid lenses (see Fig. 3), or – if a higher intensity
at the target is called for – have a small spot at the sample and refocus on the
detector position. Ideal beam dynamics for diffraction in terms of a phase
advance⁵³ approaching 90° has been found only without an intermediate focus.



45 Fig. 3 REGAE scheme. Indicated with numbers are: (1) gun cavity, (2) solenoids, (3)
collimators, (4) rebunching cavity, (5) dipole for electron energy measurements, (6)
50 target interaction chamber, and (7) detector.

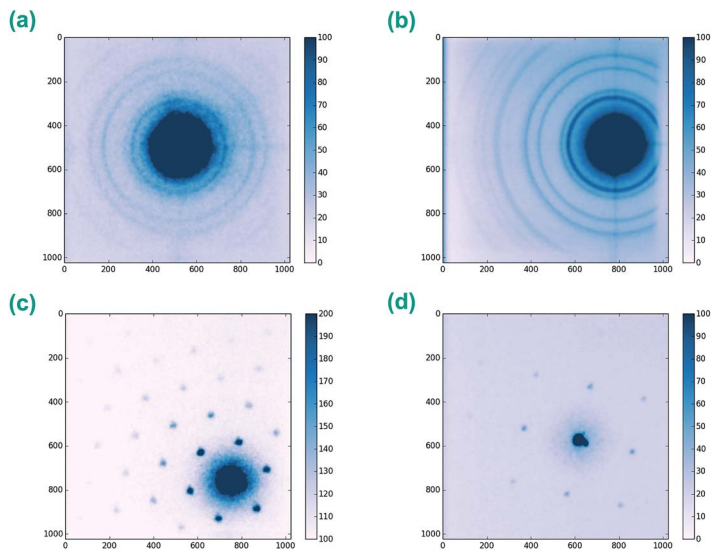


Fig. 4 Example diffraction patterns from (a, b): polycrystalline gold, (c): MoS₂, (d): Si; the quality of the diffraction is particularly notable for the single crystal samples MoS₂ and Si.

Beam size, divergence, and coherence are controlled by the photocathode and gun cavity, and transverse beam shaping elements, as solenoids, collimators and steerers. At a distance of 1.3 m from the accelerator, a rebunching cavity is placed in the beam line. It consists of four cells and is operated off-crest compared to the arrival time of the electron bunch. The rebunching cavity is driven by a fraction of the RF field that also supplies the gun. The relative phase between the cavities is adjusted with phase shifters. While the parameter space of this coupled cavity system is finite, efforts have to be made to overcome complications due to reflections and unwanted feedback between the two coupled cavities.⁵⁴ The electron bunch can, if higher acceleration is required, also be injected on-crest into the rebunching cavity. Potential beam parameters along the propagation axis are summarized in Fig. 5. For this example, the beam dynamics for a bunch of 100 fC is tracked by the ASTRA⁵⁵ simulation software, which includes space charge fields. For the initial beam parameters, we use an RMS spot size of the laser at the cathode of 10 μm , a pulse length of 0.5 ps and a charge of 100 fC. For this charge, the beam size at the target reaches 500 μm with a transverse coherence length above 10 nm. With the buncher tuned to the appropriate phase, a bunch length of 10 fs can be expected at the longitudinal focus at the sample position. We then use a solenoid close to the sample position to focus the beam and diffraction pattern to the detector. It needs to be emphasized that a pulse duration of 10 fs is sufficiently short to capture even the fastest possible nuclear motions involved in chemical processes. The achievable transverse coherence is also notable in that the design objectives were to provide sufficient transverse coherence to enable the study of systems as large as proteins. The unit cell of protein systems capable of being phototriggered to execute their biological functions such as heme proteins and the family of rhodopsin photoactive systems are on the order of 6 nm such that the transverse coherence is sufficient for this purpose.

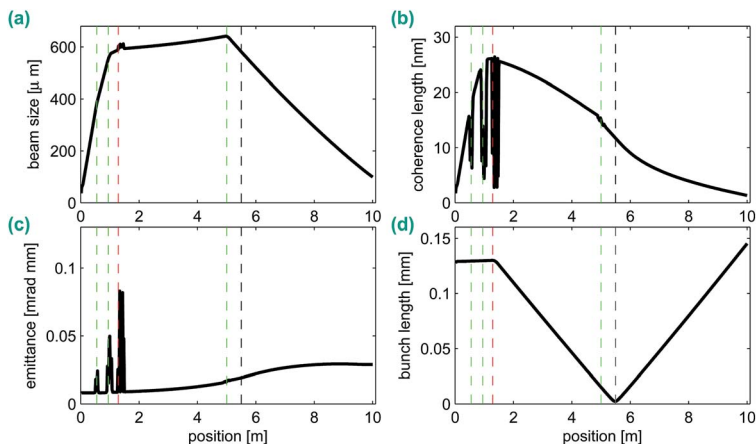


Fig. 5 ASTRA simulations for diffraction with REGAE: (a) RMS beam size showing the beam dynamics, (b) transverse coherence length, (c) emittance, and (d) bunch length in mm, corresponding to 10 fs at the longitudinal focus. The dashed lines indicate the position of solenoids (green), the rebunching cavity (red) and the sample position (black).

2.4 Static diffraction from aluminum: thickness dependence

One of the main limitations in the use of electron structural probes is the effect of multiple scattering due to the intrinsically high scattering cross-section of electrons. The increased electron penetration depth and reduced scattering angles for relativistic electrons promise the feasibility of ultra-fast electron diffraction (UED) with thick samples. In conventional electron microscopes and electron guns at intermediate energies (DC guns) typical sample thicknesses range from few tens of nanometers to 200 nm, depending on the density and atomic weight of the material. However, many interesting systems, such as protein crystals, water soluble crystalline systems, and solution phase chemistry call for a probe with a higher penetration depth. From the point of view of material science, a higher penetration depth supports the study of bulk properties with minimal effects from interfaces or surface effects. The relativistic electron energy regime has not been extensively studied and, as discussed above, only approximate relationships in terms of scaling relations for elastic and inelastic scattering are available. The effect of multiple electron scattering on image resolution needs to be explicitly determined. We explored these possibilities using films of polycrystalline aluminum of increasing thickness up to 800 nm. The calculated mean free path according to the inset in Fig. 1 is just above 200 nm. The films are supported by a 30 nm thin SiN membrane. Diffraction patterns were recorded by integrating 300 shots of 180 fC pulses at 4 MeV. Before azimuthal integration of the diffraction pattern a background image is subtracted. The incoherent contribution and the diffuse diffraction ring from the SiN membrane are modeled with a multi-component function and removed as well. These components are shown as gray lines in Fig. 6(a). The off-center peak at about 0.78 \AA^{-1} corresponds to diffuse diffraction from the supporting SiN membrane. We need to determine the effect of multiple electron scattering as a function of thickness for a given system and use the Z dependence of the scattering to provide general guidelines for limiting

1 this effect on reciprocal (diffraction) or real space resolution. Coherently scattered
electrons interfere after multiple elastic scattering, thus, the diffracted intensities
are altered compared to the single scattering regime. Inelastic scattering leads to
5 a broadening of both probe beam and diffracted electrons and can affect the
resolution. The addition of both effects is visible as an increase of diffraction ring
width, as shown in Fig. 7(c). The question whether multi-scattering effects are
necessary to describe such diffraction patterns in theoretical treatments or the
degree to which structural information is lost are still open. Modulations in
10 diffraction intensity might be averaged out in polycrystalline samples, as expected
from multi-slice calculations. To aid in resolving this issue, we compare the ratio
of diffraction intensities for different rings in Fig. 7(a) with the expected result for
a completely random powder sample, obtained from the software crystal maker.⁵⁶
The rather surprising result is that the multiple electron scattering effects, while
15 occurring, are not significantly altering the relative ratios of the different
diffraction orders as needed for dynamic structure determination. The small
deviation from ideal results is within signal to noise limits for some of the
diffraction orders. To be fully conclusive, the effect of substructure, grain size and
texture within the polycrystalline sample would need to be studied by a different
20 method.

This study gives a direct determination of the effect of multiple electron
scattering on a well-defined system. In the present case, Al is close in Z to organic
systems. We conclude that time-resolved electron diffraction studies of systems,
at least for light materials, is possible up to micrometer thickness in the rela-
25 tivistic energy range. Here is especially important to note that these experiments
always deal with systems of known structure. The experimental challenge is to be
able to discern small changes in the relative intensities of the different diffraction

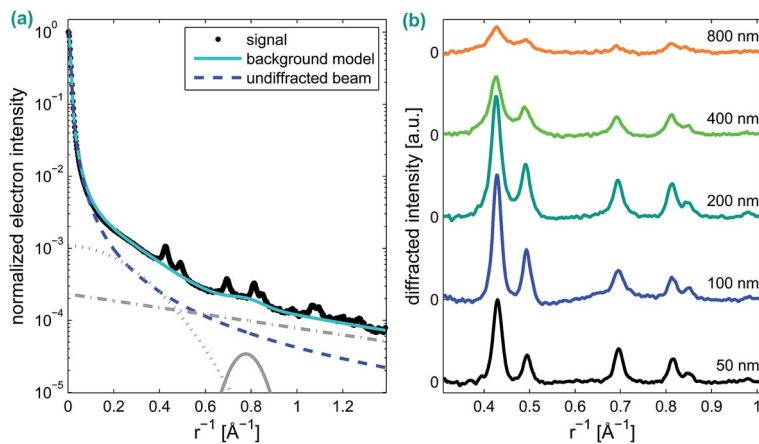


Fig. 6 (a) Example for electron diffraction from poly-crystalline aluminum film after azimuthal integration. The signal (black) has been normalized to the transmitted peak intensity. A reference image including dark current has been subtracted before integration. Further subtraction removes the un-diffracted beam (dashed blue line) and incoherent background (solid blue line) from the coherently diffracted signal. Incoherent contributions are shown in grey. (b) Diffracted intensity after background subtraction. The diffraction patterns are stacked for better visibility.

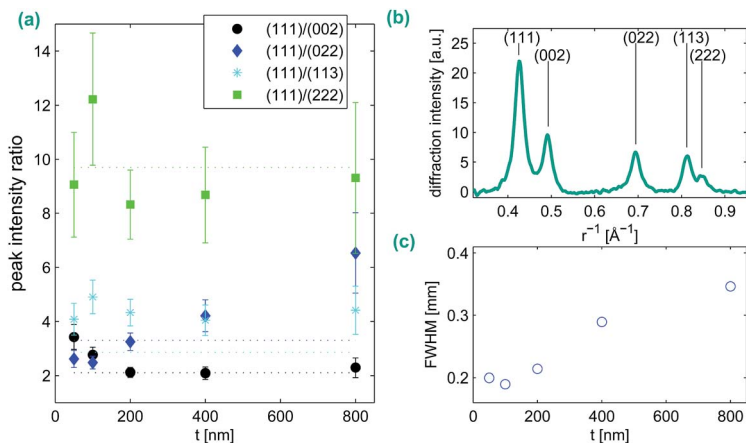


Fig. 7 (a) Ratio of peak intensities in diffraction pattern. The dashed lines gives the scattering ratio for a perfect powder sample in the single scattering regime for comparison. An example diffraction pattern for 200 nm thickness is shown in (b), where the integrated diffraction rings are labeled with Miller indices. (c) Width of rings in diffraction pattern with increasing thickness.

orders. This control study shows that it is possible to extract structural dynamics from samples as thick as several hundred nanometers to micron thickness at this energy range. This feature of relativistic electrons was one of the primary motivations for developing this source as it dramatically increases the ease of sample preparation and opens up solution phase chemistry to atomic inspection, which is much easier to realize with micron scale path lengths as opposed to 100 nm needed for nonrelativistic electron studies.

3 Ultrafast dynamics with REGAE

3.1 Finding $t = 0$

In order to perform time-resolved electron diffraction studies, one needs to characterize the instrument's time resolution. Before such studies can be performed in detail however, the temporal overlap ($t = 0$) between pump and probe, in our case excitation laser and electron pulse, needs to be found. Here, a process that is reversible under photoexcitation is favorable. We used the laser induced plasma formation as a means to determine the electron-laser timing using a copper mesh at the target position with an incident fluence of 14.9 mJ cm^{-2} . Images of the mesh are acquired on the detector in transmission mode. The magnification is close to one, so that the lines with a spacing of $24.5 \text{ }\mu\text{m}$ are not resolved in these images. Similar experiments have been presented in.⁵⁷ Examples of images prior to and after laser irradiation are shown in Fig. 8(a) and (b). The excitation laser with a width of $500 \text{ }\mu\text{m}$, a wavelength of 800 nm and a pulse width of $\approx 80 \text{ fs}$ induces a plasma in the center of the mesh, from where a charged plume is expelled. The probe electron beam is partially deflected by this spatial gradient in charge, which can be observed as the depleted area in the electron density distribution, as depicted in Fig. 8(b). The electron beam seems to be affected on a smaller area than expected from the laser beam size, which we

interpret as higher order absorption processes in the high intensity center of the laser beam. The higher order multi photon absorption processes lead in turn to a reduction in the effective beam diameter giving rise to the observed effect. The excitation arrival time was varied using a delay stage and a series of shadow images was recorded scanning through the time delay between the laser excitation and electron probe pulses. In order to retrieve $t = 0$ from the shadow images, we analyzed the RMS intensity changes in the central area of the beam. As plotted in Fig. 8(c), we observed a step in the signal, the onset of which is assumed to indicate the zero – time point. Furthermore, we evaluated the width of the differential change in intensity and find a FWHM of 0.9 ps where the changes are occurring fastest in the center of the imaged profile. The result indicates that the electron bunch length is in the sub picosecond range.

3.2 Laser induced structural dynamics of gold

The first structural dynamics at REGAE were observed in a similar geometry to that used for the plasma studies, but under single shot conditions. Free standing membranes of polycrystalline gold were used to observe a laser induced structural change. The membranes with a size of $200\ \mu\text{m}$ by $200\ \mu\text{m}$ were excited one by one with a laser pulse, and the resultant diffraction images were recorded. At a fluence of $150\ \text{mJ cm}^{-2}$ and 100 fs pulse duration, the excitation leads to melting and therefore damage of the sample, and is not reversible. For the data presented here, 300 of these membranes fabricated on a chip were used. Again, example images before and after laser irradiation are shown in Fig. 9(a) and (b).

The diffraction image after laser irradiation still exhibits diffraction rings, but the amplitude of the outer rings is diminished. This change indicates a loss of long range order due to melting of the sample. The timescale of this change from ordered to a disordered state is shown in Fig. 9(c). Here, the diffraction rings' amplitudes are plotted *versus* delay time between laser and electron bunch. Each time step was repeated three times. Within five picoseconds after excitation, the outer rings are fading, while the ring indexed with (111) gains in intensity. This gain is attributed to an overlap of the (111) diffraction ring and diffraction from a liquid state. At longer delay times we find the sample completely destroyed. The above results are the first time-resolved studies of REGAE that clearly show its capabilities for single shot structure determination on the 100 fs time scale. The

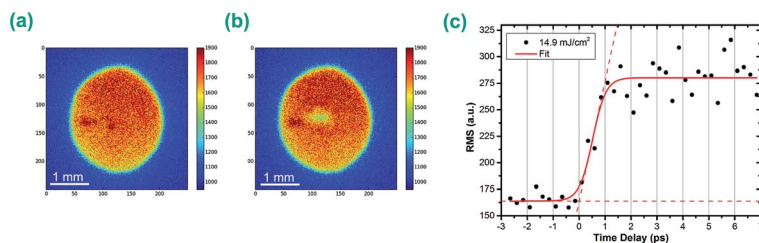


Fig. 8 Shadow images of a copper mesh before (a) and after (b) laser irradiation. The deflection of the electron bunch can be observed as a depleted region in the electron beam profile. The analysis of the signal is shown in (c): the signal RMS in the central region is evaluated and shows a step with a time constant of 0.9 ps.

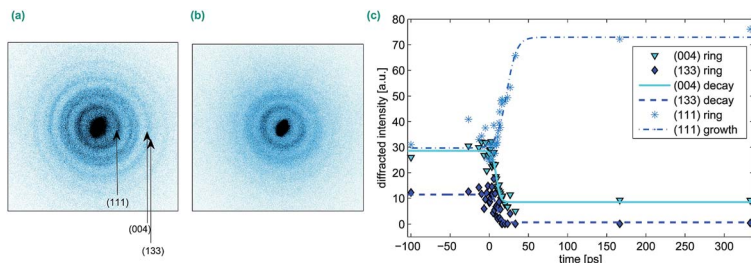


Fig. 9 Single shot diffraction patterns before (a) and after (b) laser excitation. (c) Intensity of the diffraction rings as a function of time delay between pump and probe pulse.

observed dynamics for the particular fluences match very well those found earlier.⁵⁸ The present time resolution is limited by RF timing issues and it must be stated that this limit is primarily due to problems in finding a suitably fast reference system to optimize the phase of the rebunching cavity for optimal compression. The best solution will be to introduce an RF streak camera for enabling optimization of the pulse compression process (in progress). This diagnostic tracks the phase jitter of the RF so it is not suitable for jitter compensation between the RF and the laser excitation. However, by simultaneously recording the central beam position with the high dynamic range detector, it will be possible to achieve an overall time resolution in the 10 fs range, as demonstrated using phototriggered streak cameras for time stamping and correction of the jitter.^{26–29}

4 Concluding remarks

The present space-time limitations have been increased to the 10 femtosecond time scale with changes in intensity in diffraction orders corresponding to net atomic displacements of less than 0.05 \AA with single shot capabilities. This space-time resolution is sufficient now to capture the fastest nuclear motions involved in chemistry. In this respect, the single most restrictive condition on space-time resolution, not discussed within the context of the electron source physics, is the sample constraints. The use of electron structural probes to provide table top high brightness sources by its nature requires very thin samples, on the order of few 10 s of nanometers to 100 nm scale for nonrelativistic electrons. It is the sample limitations that impose the brightness condition in the first place. These are precious samples in which excitation induced damage and thermal effects limiting sampling rate have dictated the need for ultrabright sources. There are some samples however that are just not amenable to such short path lengths. Two prime examples of great interest are solution phase chemistry and protein dynamics. Although, there have been major advances in the development of nanofluidics for this expressed purpose,^{59,60} it is much simpler to use micron scale flow conditions to achieve the desired flow rates for sample exchange. Similarly for protein systems, the highest spatial resolution is achieved in diffraction and the functionally relevant motions involving the protein are spatially distributed leading to very small net RMS atomic motions, yet are central to the proteins role in transducing stored chemical potential into function.⁴ If we are ever to make the

1 key connections between correlated motions inherent to particular protein
structures or motifs as part of a generalized understanding of protein structure–
function correlations, we will need to make these observations in diffraction. All
5 protein crystals are water soluble and as such are not amenable to classic
microtome methods to fabricate 100 nm thin slices needed for nonrelativistic
electron probes. Herein is the major advantage of relativistic electrons over lower
energy sources. There are scaling relations for the electron mean free path that
10 indicate higher energy electrons will enable the use of thicker samples. However,
the difference inelastic and elastic scattering need to be determined as there are
approximations as is evident from the noted differences between experimental
measurements and calculated scattering cross-sections. Most important, sample
15 quality has an enormous influence on spatial resolution (*vide infra*). In the present
work, we have conducted a systematic study of the effect of sample thickness on
the apparent structure resolution. By comparing both experiment and theoretical
calculations based on multi slice methods for dealing with multiple electron
scattering, we find that it is possible to use samples up to thicknesses of nearly 1
20 micron for materials of low Z corresponding to the range of most organic and
biological systems of interest. This finding also means that it should be possible
to dramatically relax the engineering requirements for introducing flowing liquid
cells with electron transparent SiN windows. In terms of spatial resolution limits
for discerning structural changes, it is important to emphasize further that the
25 measurement does not have the same requirements as needed to resolve a
previously unknown structure. The experiment relies on knowing the initial and
in most cases final structure and observing the differential displacements in
atomic positions that connect one structure to another. This observation gives us
directly information on the key modes coupled to the reaction coordinate and
enables observation of the reduction in dimensionality that occurs in curve cross
30 regions between reactant and product surfaces. This feature is central to chem-
istry and it is this enormous reduction in dimensionality in barrier or curve
crossing regions that ultimately makes chemistry a transferable concept. These
relatively small but highly correlated motions are observable as long as the rela-
tive ratios of the various diffraction orders is conserved and within the dynamic
35 range of the structurally induced changes in intensity. We therefore conclude that
it will be possible to pull out the structural changes for many classes of time-
resolved diffraction experiments, involving samples that were previously
thought intractable due to either their liquid nature or sample thickness issues.
This finding that multiple electron scattering is not as big an effect as sample
40 quality and attenuation with sample thickness has enormous implications for
improving sample preparation methods. This study also reaffirms the primary
motivation for the development of relativistic electron sources for atomically
resolved structural dynamics as this source greatly relaxes sample requirements
for all classes of study. Future investigations comparing data to calculated
45 diffraction patterns will give more insight into the sensitivity that is required to
further confirm our observation.

In terms of space-time resolution, relativistic sources also offer the highest
possible source brightness for a given photocathode. The high-Q RF cavities
50 provide the highest possible field gradients to accelerate the electron bunch up to
the relativistic regime prior to any excessive space-charge broadening effects can
spoil the space time correlation of the electrons in the accelerating field. This

1 condition is central to the use of rebunching cavities to correct the small velocity
spread from the field gradient. As shown in the present work, based largely on
well tested simulations, pulses as short as 10 fs with electron bunch charges of 10^6
5 to 10^7 electrons per pulse for typical matching electron beam to laser excitation
beam parameters are achievable. It should be noted that there is a great deal of
effort to further increase field gradients for next generation electron accelerators
and light sources. The use of extremely high peak power few cycle THz pulses has
recently been demonstrated to give uniform acceleration and deceleration of
10 nonrelativistic seed electrons with estimated field gradients in excess of 1 GV m^{-1}
or more than an order of magnitude larger than the best RF cavities.⁶¹ This
development would lead to correspondingly shorter electron pulses for a given
bunch density. With respect to improving time resolution, concepts similar to
streaking with RF deflecting structures might be implemented in the future as
well.⁶²

15 The most important advances in electron source brightness will deal with the
transverse coherence limitations. The present photo cathodes typically have
initial transverse energy spreads of 0.2 to 0.6 eV. This initial energy spread is the
greatest limiting factor in the transverse coherence and ability to image complex
20 molecular systems such as proteins. Even within this range of transverse
momentum spread, it has been possible to now track atomic motions for large
molecular systems with unit cells of $>3 \text{ nm}$ that are comparable to unit cells of
many important protein systems.⁶³ Further decreases in transverse momentum
spread will make higher resolution of even minute motions as well as scaling to
25 larger and more complex systems. In this respect, the use of ultracold atom
sources using threshold ionization of Rydberg states have given results close to
the theoretical quantum limit for fermions with respect to the minimum transverse
velocity spread, yielding effective electron temperatures of 10 K or less than
0.6 meV.⁴¹ This approach, however, is limited in electron density by the relatively
30 low atom density achievable in ultracold atom traps. In order to get sufficient
electron numbers for near single shot conditions, the initial beam size
approaches mm dimensions that cancel the net reduction in emittance. The
electron beam is indeed very cold but the angular distribution does not lead to
much improvement in the transverse coherence at the sample position due to the
35 very large source size at the photocathode. We contend that the brightest photo
cathodes will still be based on solid state cathodes. Significant progress has been
made lately in understanding the scattering issues and boundary conditions for
photoemission from solid state systems. Recent studies of trialkali photo cathodes
40 have given evidence for thermally limited photoemission with energy
spreads of 160 meV at room temperature,⁶⁴ and factors of 10 reduction are clearly
possible with excitation closer to threshold. These photo cathodes also enjoy
relatively high quantum yields as found for other semiconductor photo cathodes
such as the routinely used CsTe materials. Although it is not straightforward, it
45 should be possible to use cryogenically cooled solid state photo cathodes. The
challenge is to thermally isolate the cathode section of the electron gun while still
having sufficient conduction to avoid excessive charge build up and break down
at the high fields used for extraction. It should nevertheless be possible to go to 10
K for suitable source sizes that would give an increase in source brightness of
50 approximately 2 orders of magnitude over the commonly used photo cathodes in
femtosecond electron diffraction studies. In this event, it will be possible to scale

1 up the experiments to the study of effectively any molecular system and relevant
biological systems.

2 The above technical achievements could be made in the relatively short term.
3 As with all experiments aimed at structure determination, the quality of the
4 sample ultimately dictates the limits. Future efforts will need to focus on new
5 methods of introducing samples into the vacuum environment of electron
diffraction or real space imaging systems. With the relatively recent advent of
6 nanotechnology into this domain, there is reason to believe that it will soon be
possible to introduce large arrays of crystals, with the potential for M-pixel arrays
7 of nanocrystals into the sample chambers. High throughput methods developed
for XFEL experiments could also be adopted for electron use with appropriate
8 design of environmental enclosures around the sample viewing area. Ion milling
and *in situ* growth of 2D crystals and nanocrystals will need to be explored.¹⁹ In all
9 cases, the lessons learned in increasing source brightness will pay enormous
dividends for increasing the spatial resolution using electrons for static structure
10 determinations and the importance of these advances should not be undervalued.
In the end, it will be the sample that will dictate the space-time resolution limits –
11 as it should be.

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